

Wiskunde Anibrand

Antwoordboek Graad 8

Annie Bothma

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Graad 8 Antwoordboek opgestel deur A Bothma

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Hoofstuk 1

Getalle, Bewerkings en Verwantskappe

Antwoorde 1A: Getallestelsels gr 8

1.

Getal	\mathbb{R}	\mathbb{Q}'	\mathbb{Q}	\mathbb{Z}	\mathbb{N}_o	\mathbb{N}
$-5\frac{2}{3}$	✓		✓			
3,2574	✓		✓			
$\sqrt{16} = 4$	✓		✓	✓	✓	✓
$\sqrt{15} = 3,87\dots$	✓	✓				
-2	✓		✓	✓		
$\pi = 3,141\dots$	✓	✓				
$\frac{22}{7}$	✓		✓			
$-0,3 = \frac{3}{10}$	✓		✓			
8,2543....	✓	✓				

2.1 $\sqrt{35} = 5,916079\dots$
 $\simeq 5,916$

2.2 $\sqrt[3]{12} = 2,289428\dots$
 $\simeq 2,289$

2.3 $\pi = 3,141592\dots$
 $\simeq 3,142$

2.4 $5\pi = 15,7079632679$
 $\simeq 15,708$

2.5 $\frac{7\pi}{3} = 7,33038285838$
 $\simeq 7,330$

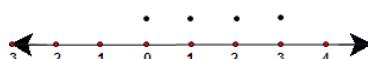
2.6 $\pi + 9 = 12,141592\dots$
 $\simeq 12,142$

2.7 $7\sqrt{10} = 22,135943\dots$
 $\simeq 22,136$

2.8 $\frac{\sqrt[3]{65}}{12} = 0,335060\dots$
 $= 0,335$

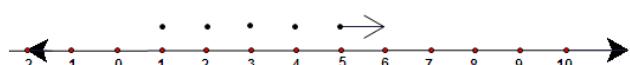
3.1 Getabelleerd: $\{0;1;2;3\}$

Grafies: **Onthou telgetalle begin by 0**



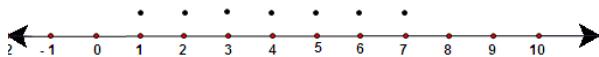
3.2 Getabelleerd: $\{1;2;3;\dots\dots\dots\}$

Grafies: **Onthou natuurlike getalle begin by 1**



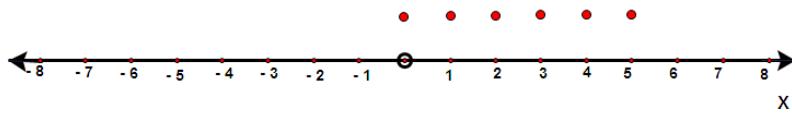
3.3 Getabelleerd: $\{1; 2; 3; 4; 5; 6; 7\}$

Grafies:



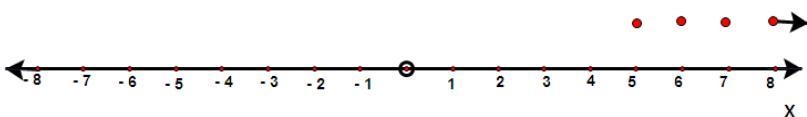
3.4 Getabelleerd: $\{0; 1; 2; 3; 4; 5\}$

Grafies: **Onthou telgetalle begin by 0**



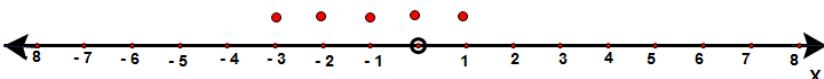
3.5 Getabelleerd: $\{5; 6; 7; 8; \dots\}$

Grafies: **Onthou natuurlike begin by 1**



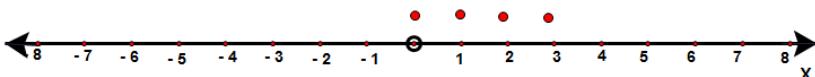
3.6 Getabelleerd: $\{-3; -2; -1; 0; 1\}$

Grafies:



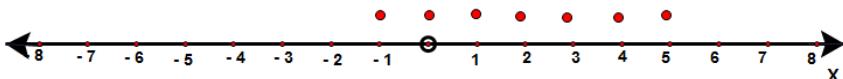
3.7 Getabelleerd: $\{0; 1; 2; 3\}$

Grafies: **Onthou telgetalle begin by 0**



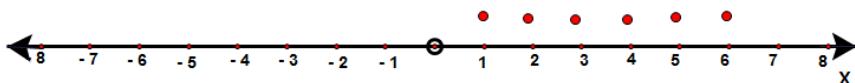
3.8 Getabelleerd: $\{-1; 0; 1; 2; 3; 4; 5\}$

Grafies:



3.9 Getabelleerd: $\{1; 2; 3; 4; 5; 6\}$

Grafies: **Onthou natuurlike begin by 1**



3.10 Getabelleerd: $\{-1; 0; 1; 2; \dots\}$

Grafies:



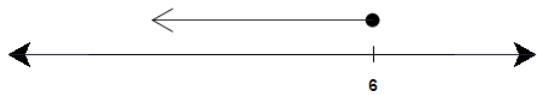
3.11 Geen tabellering

Grafies:



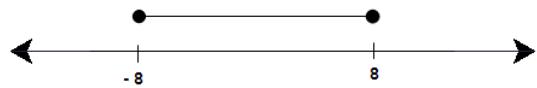
3.12 Geen tabellering

Grafies:



3.13 Geen tabellering

Grafies:



3.14 Geen tabellering

Grafies:



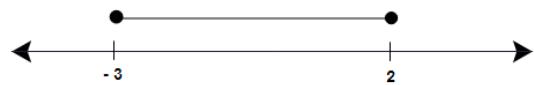
3.15 Geen tabellering

Grafies:



3.16 Geen tabellering

Grafies:



3.17 Geen tabellering

Grafies:



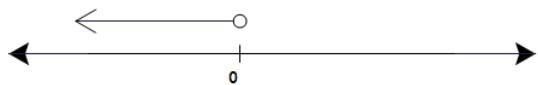
3.18 Geen tabellering

Grafies:



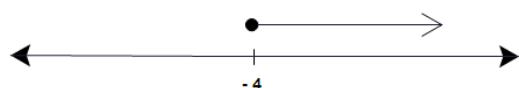
3.19 Geen tabellering

Grafies:



3.20 Geen tabellering

Grafies:



4.

Getal	\mathbb{N}	\mathbb{N}_0	\mathbb{Z}	\mathbb{Q}	\mathbb{Q}'	\mathbb{R}	nie- \mathbb{R}
Bv. $-5\frac{2}{3} = \frac{-17}{3}$	✗	✗	✗	✓	✗	✓	✗
2,813	✗	✗	✗	✓	✗	✓	✗
4, i	✗	✗	✗	✓	✗	✓	✗
$\sqrt{-25}$	✗	✗	✗	✗	✗	✗	✓
$\sqrt[3]{-27} = -3$	✗	✗	✓	✓	✗	✓	✗
3π	✗	✗	✗	✗	✓	✓	✗
$\sqrt{15} = 3,872\dots$	✗	✗	✗	✗	✓	✓	✗
$\sqrt{36+64} = \sqrt{100} = 10$	✓	✓	✓	✓	✗	✓	✗
81,24873....	✗	✗	✗	✗	✓	✓	✗
$-\sqrt{100} = -10$	✗	✗	✓	✓	✗	✓	✗
$0 \div 36 = 0$	✗	✓	✓	✓	✗	✓	✗

5. $\pi = 3,141\dots$; $1,6\dot{5}$; $\sqrt[3]{64} = 4$; $\sqrt{82} = 9,055\dots$; $\frac{22}{7}$; $\sqrt{-36}$; $1,2435\dots$

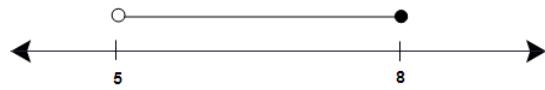
5.1 π ; $\sqrt{82}$; $1,2435\dots$

5.2 $\sqrt{-36}$

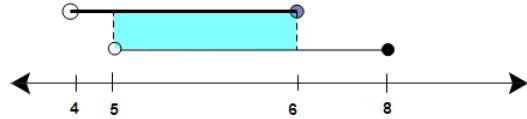
6.1



6.2

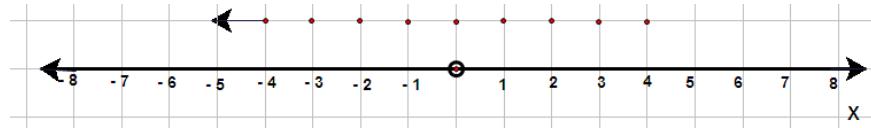


6.3

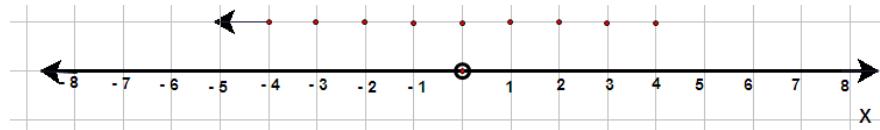


Al die reële getalle groter as 5 en kleiner en gelyk aan 6

7. $x < 5$ en $x \in \mathbb{Z}$



8. $-2 < x \leq 8$ en $x \in \mathbb{R}$



Hoofstuk 1

Getalle, Bewerkings en Verwantskappe

Antwoorde 1B: Veelvoude, faktore en priemgetalle

1. $A = \{1; 2; 3; 4; \dots; 30\}$
- 1.1 $F_{18} = \{1; 2; 3; 6; 9; 18\}$ 1.2 Priemfaktore₁₈ = {2; 3}
- 1.3 $V_9 = \{9; 18; 27\}$ 1.4 {2; 3; 5; 7; 11; 13; 17; 19; 23; 29}
- 1.5 {2}
- 1.6 {4; 6; 8; 9; 10; 12; 14; 15; 16; 18; 20; 21; 22; 24; 25; 26; 27; 28; 30}
2. $V_6 = \{6; 12; 18; 24; 30; 36; 42; 48; 54; 60; 66; 72; 78; 84; \dots\}$
 V_6 tussen 35 en 80 = {36; 42; 48; 54; 60; 66; 72; 78}
- 3.1 $1 \times 60; 2 \times 30; 3 \times 20; 4 \times 15; 5 \times 12; 6 \times 10$
 $F_{60} = \{1; 2; 3; 4; 5; 6; 10; 12; 15; 20; 30; 60\}$
- 3.2 $PF_{60} = \{2; 3; 5\}$
- 3.3 $SF_{60} = \{4; 6; 10; 12; 15; 20; 30; 60\}$
4. Dit is 'n getal wat meer as 2 faktore het.
5. $1 \times 36; 2 \times 18; 3 \times 12; 4 \times 9; 6 \times 6$
 $F_{36} = \{1; 2; 3; 4; 6; 9; 12; 18; 36\}$
 $SF_{36} = \{4; 6; 9; 12; 18; 36\}$
- 6.1 $F_{36} = \{1; 2; 3; 4; 6; 9; 12; \mathbf{18}; 36\}$
 $1 \times 54; 2 \times 27; 3 \times 18; 6 \times 9$
 $F_{54} = \{1; 2; 3; 6; 9; \mathbf{18}; 27; 54\}$
- 6.2 GGF = 18
- 7.1 $V_{12} = \{12; 24; \mathbf{36}; 48; 60; 72; 84; 96; 108; 120\}$
 $V_{18} = \{18; \mathbf{36}; 54; 72; 90; 108; 126; 144; 162; 180\}$
- 7.2 KGV = 36
- 8.1 $24 = 2 \times 2 \times 2 \times 3$
- 8.2 $63 = 3 \times 3 \times 7$
- 8.3 $2 \mid 360$ 8.4 $3 \mid 3465$
 $2 \mid 180$ $3 \mid 1155$
 $2 \mid 90$ $5 \mid 385$
 $3 \mid 45$ $7 \mid 77$
 $3 \mid 15$ $11 \mid 11$
 $5 \mid 5$ $\mid 1$
 $\mid 1$ $3465 = 3 \times 3 \times 5 \times 7 \times 11$
- $360 = 2 \times 2 \times 2 \times 3 \times 3 \times 5$

8.5 $2 \mid 588$
 $2 \mid 294$
 $3 \mid 147$
 $7 \mid 49$
 $7 \mid 7$
 $\quad \quad \quad \lfloor 1$

$$588 = 2 \times 2 \times 3 \times 7 \times 7$$

8.6 $\frac{1800}{5400}$ $2/1800$ $2/5400$
 $= \frac{2^3 \times 3^2 \times 5^2}{2^3 \times 3^3 \times 5^2}$ $2/900$ $2/2700$
 $= \frac{1}{3}$ $2/450$ $2/1350$
 $\quad \quad \quad 3/225$ $3/675$
 $\quad \quad \quad 3/75$ $3/225$
 $\quad \quad \quad 5/25$ $3/75$
 $\quad \quad \quad 5/5$ $5/25$
 $\quad \quad \quad 1$ $5/5$
 $\quad \quad \quad \quad \quad \quad 1$

9.1 $2 \mid 112$ $2 \mid 210$
 $2 \mid 56$ $3 \mid 105$
 $2 \mid 28$ $5 \mid 35$
 $2 \mid 14$ $7 \mid 7$
 $7 \mid 7$ $\lfloor 1$
 $\quad \quad \quad \lfloor 1$

$$112 = \cancel{2} \times 2 \times 2 \times 2 \times \cancel{7}$$

$$210 = \cancel{2} \times 3 \times 5 \times \cancel{7}$$

$$\text{GGF} = 2 \times 7 = 14$$

9.2 $2 \mid 38$ $3 \mid 57$ $5 \mid 95$
 $19 \mid 19$ $19 \mid 19$ $19 \mid 19$
 $\lfloor 1$ $\lfloor 1$ $\lfloor 1$

$$38 = 2 \times 19$$

$$57 = 3 \times 19$$

$$95 = 5 \times 19$$

$$\text{GGF} = 19$$

9.3

$$2 \lfloor 12$$

$$2 \lfloor 6$$

$$3 \lfloor 3$$

$$\lfloor 1$$

$$2 \lfloor 168$$

$$2 \lfloor 84$$

$$2 \lfloor 42$$

$$3 \lfloor 21$$

$$7 \lfloor 7$$

$$\lfloor 1$$

$$12 = (2 \times 2) \times 3$$

$$168 = (2 \times 2) \times 2 \times 3 \times 7$$

$$\text{GGF} = 2 \times 2 \times 3 = 12$$

$$9.4 \quad 15 = 3 \times 5 \quad 45 = 9 \times 5 = 3 \times 3 \times 5 \quad 60 = 6 \times 10 = 2 \times 3 \times 2 \times 5$$

$$15 = (3 \times 5)$$

$$45 = 3 \times 3 \times 5$$

$$60 = 2 \times 2 \times 3 \times 5$$

$$\text{GGF} = 3 \times 5 = 15$$

$$10. \quad 14 = 2 \times 7 \quad 28 = 4 \times 7 = 2 \times 2 \times 7 \quad 42 = 6 \times 7 = 2 \times 3 \times 7$$

$$14 = (2 \times 7)$$

$$28 = (2 \times 2 \times 7)$$

$$42 = (2 \times 3 \times 7)$$

$$\text{GGF} = 2 \times 7 = 14$$

$$11.1 \quad 9 = 3 \times 3 \quad 24 = 4 \times 6 = 2 \times 2 \times 2 \times 3$$

$$9 = (3 \times 3)$$

$$24 = (2 \times 2 \times 2) \times 3$$

$$\text{KGV} = 3 \times 3 \times 2 \times 2 \times 2 = 72$$

$$11.2 \quad 6 = 2 \times 3 \quad 12 = 4 \times 3 = 2 \times 2 \times 3 \quad 18 = 2 \times 9 = 2 \times 3 \times 3$$

$$6 = (2 \times 3)$$

$$12 = 2 \times (2 \times 3)$$

$$18 = 2 \times 3 \times (3)$$

$$\text{KGV} = 2 \times 3 \times 2 \times 3 = 36$$

$$11.3 \quad 19 = 1 \times 19 \quad 38 = 2 \times 19 \quad 76 = 2 \times 38 = 2 \times 2 \times 19$$

$$19 = 1 \times 19$$

$$38 = 2 \times 19$$

$$76 = 2 \times 2 \times 19$$

$$\text{KGV} = 19 \times 2 \times 2 = 76$$

$$2|270$$

$$\begin{array}{rcl} 11.4 \quad 3|15 & 3|45 & 3|135 \\ 5|5 & 3|15 & 3|45 \\ \lfloor 1 & 5\lfloor 5 & 3\lfloor 15 \\ & \lfloor 1 & 5\lfloor 5 \\ & & \lfloor 1 \end{array}$$

$$3 = (3 \times 5)$$

$$45 = 3 \times (3 \times 5)$$

$$270 = (2 \times 3 \times 3 \times 3) \times 5$$

$$\text{KGV} = 3 \times 5 \times 3 \times 2 \times 3 = 270$$

12. Veelvoude van $\frac{1}{2}$ (tel in halwes): $\frac{1}{2}; \frac{2}{2} = 1; \frac{3}{2}; \frac{4}{2}; \dots$

Veelvoude van $\frac{1}{3}$ (tel in derdes): $\frac{1}{3}; \frac{2}{3}; \frac{3}{3} = 1; \frac{4}{3}; \frac{5}{3}; \dots$

Veelvoude van $\frac{1}{4}$ (tel in kwartes): $\frac{1}{4}; \frac{2}{4} = \frac{1}{2}; \frac{3}{4}; \frac{4}{4} = 1; \frac{5}{4}; \frac{6}{4}; \dots$

KGV van $\frac{1}{2}, \frac{1}{3}$ en $\frac{1}{4} = 1$

13 Ons soek die KGV van 12, 18 en 30

$$12 = 2 \times 6 = 2 \times 2 \times 3 \quad 18 = 2 \times 9 = 2 \times 3 \times 3 \quad 30 = 6 \times 5 = 2 \times 3 \times 5$$

$$12 = (2 \times 2 \times 3)$$

$$18 = 2 \times 3 \times (3)$$

$$30 = 2 \times 3 \times (5)$$

$\text{KGV} = 2 \times 2 \times 3 \times 3 \times 5 = 180$, dus na 180 sekondes sal die 3 klokke weer saam lui.

14. 53124 deelbaar deur 2, 3, 4, 5 en 6

- Is deelbaar deur 2, want die laaste syfer is 4 wat ewe is.
- Is deelbaar deur 3, want die som van die syfers is $5 + 3 + 1 + 2 + 4 = 15$ en 15 is deelbaar deur 3
- Is deelbaar deur 4, want die laaste twee syfers gee die getal 24 wat deelbaar is deur 4
- Is nie deelbaar deur 5, want die laaste syfer is nie 'n 0 of 'n 5
- Is deelbaar deur 6, want dit is deelbaar deur beide 2 en 3

15. 487245 deelbaar deur 2, 3, 4, 5 en 6

- Is nie deelbaar deur 2, want die laaste syfer is 5 wat nie ewe is nie.
- Is deelbaar deur 3, want die som van die syfers is $4 + 8 + 7 + 2 + 4 + 5 = 30$ en 30 is deelbaar deur 3
- Is nie deelbaar deur 4, want die laaste twee syfers gee die getal 45 wat nie deelbaar is deur 4
- Is deelbaar deur 5, want die laaste syfer is 'n 5
- Is nie deelbaar deur 6, want dit is deelbaar deur beide 3 maar nie deur 2

16.1 1 is 'n priemgetal - verkeerd, want dit het net 1 faktor nie 2 nie.

16.2 12 is 'n veelvoud van 36 - verkeerd, want 36 is 'n veelvoud van 12

16.3 $\sqrt{64+36} = 8+6=14$ - verkeerd want $\sqrt{64+36} = \sqrt{100} = 10$

16.4 Die priemfaktore van 24 is 2 en 3 - korrek.

16.5 2 is 'n saamgestelde getal - verkeerd, dit is priem.

16.6 Die GGD of GGF van 5 en 10 is 10 - verkeerd. $F_5 = \{1; 5\}$ en $F_{10} = \{1; 2; 5; 10\}$, dus GGF = 5

16.7 Die KGV van 5 en 10 is 10 - korrek. $V_5 = \{5; 10; 15; 20; \dots\}$ en $V_{10} = \{10; 20; 30; 40; \dots\}$. KGV = 10

16.8 Alle onewe getalle is priemgetalle - verkeerd, want bv 9 is onewe maar nie priem nie

$$\begin{array}{r} 2|154 \\ 7|77 \\ 11|11 \\ \quad |1 \\ \hline 154 = 2 \times 7 \times 11 \end{array} \qquad \begin{array}{r} 2|98 \\ 7|49 \\ 7|7 \\ \quad |1 \\ \hline 98 = 2 \times 7 \times 7 \end{array}$$

$$\text{GGF} = 2 \times 7 = 14 \qquad \text{KGV} = 2 \times 7 \times 11 \times 7 = 1078$$

18. $V_{16} = \{16; 32; 48; 64; 80; 96; 112; 128; 144\}$

$$V_{18} = \{18; 36; 54; 72; 90; 108; 126; 144\}$$

$$\text{KGV} = 144$$

Kortste stuk draad is **144cm**

Jy kan ook leertjie metode gebruik om KGV te bepaal.

19.

- 2 kan in 2160 indeel want die laaste syfer van die getal is ewe (0)
- 3 kan in 2160 indeel want die som van die syfers is $2 + 1 + 6 + 0 = 9$ en 9 is deelbaar deur 3
- 4 kan in 2160 indeel want die laaste 2 syfers vorm die getal 60 wat deelbaar is deur 4
- 5 kan in 2160 indeel want die laaste syfer van die getal is 0
- 6 kan in 2160 indeel want die getal is deelbaar deur 2 en 3
- 8 kan in 2160 indeel want die laaste 3 syfers vorm die getal 160 wat deelbaar is deur 8
- 9 kan in 2160 indeel want die som van die syfers is $2 + 1 + 6 + 0 = 9$ en 9 is deelbaar deur 9

20. Ons moet die GGF of GGD van 54 en 42 vind. Dit sal die vierkant se sylengte gee, sodat hierdie vierkant presies in die lengte en breedte van die karton sal inpas

$$\begin{array}{r} 2|54 \\ 3|27 \\ 3|9 \\ 3|3 \\ \quad |1 \\ \hline 54 = 2 \times 3 \times 3 \times 3 \end{array} \qquad \begin{array}{r} 2|42 \\ 3|21 \\ 7|7 \\ \quad |1 \\ \hline 42 = 2 \times 3 \times 7 \end{array}$$

$$\begin{aligned} 54 &= (2 \times 3) \times 3 \times 3 \\ 42 &= (2 \times 3) \times 7 \end{aligned}$$

GGF of GGD van 54 en 42 is $2 \times 3 = 6$

\therefore Die sylengte van die vierkant moet **6cm** wees.

21.1 $F_{60} = \{1; 2; 3; 4; 5; 6; 10; 12; 15; 20; 30; 60\}$

21.2 $PF_{60} = \{2; 3; 5; \}$

21.3 $60^2 = 3600$

21.4 Vierkantsgetalle kleiner as $60 = \{1; 4; 9; 16; 25; 36; 49\}$

22. 2160

2 deel in want 0 is ewe

3 deel in want $2 + 1 + 6 + 0 = 9$ wat deelbaar is deur 3

4 deel nie in nie, want 60 is nie deelbaar deur 4 nie

5 deel in want die laaste syfer is 0

6 deel in want getal is deelbaar deur 2 en 3

8 deel in want 160 is deelbaar deur 8

9 deel in want $2 + 1 + 6 + 0 = 9$ wat deelbaar is deur 9

Hoofstuk 1

Getalle, Bewerkings en Verwantskappe

Antwoorde 1C: Eksponente en Wetenskapnotasie

$$1.1 \quad 3^5 = 3 \times 3 \times 3 \times 3 \times 3$$

$$1.2 \quad 4^6 = 4 \times 4 \times 4 \times 4 \times 4 \times 4$$

$$1.3 \quad 2^4 \times 7^3 = 2 \times 2 \times 2 \times 2 \times 7 \times 7 \times 7$$

$$1.4 \quad (5^3)^4 = 5^3 \times 5^3 \times 5^3 \times 5^3$$

$$= (5 \times 5 \times 5) \times (5 \times 5 \times 5) \times (5 \times 5 \times 5) \times (5 \times 5 \times 5)$$

$$2.1 \quad 2 \times 2 \times 2 \times 2 \times 2 \times 2 = 2^6$$

$$2.2 \quad 10 \times 10 \times 10 \times 10 = 10^4$$

$$2.3 \quad 3 \times 3 \times 3 \times 3 \times 3 \times 7 \times 7 = 3^5 \times 7^2$$

$$2.4 \quad \frac{5 \times 5 \times 5 \times 5 \times 5 \times 5}{11 \times 11 \times 11 \times 11} = \frac{5^6}{11^4}$$

$$3.1 \quad 5^3 \times 5^4 = 5 \times 5 \times 5 \times 5 \times 5 \times 5 \times 5 = 5^7$$

$$3.2 \quad \frac{7^5}{7^3} = \frac{7 \times 7 \times 7 \times 7 \times 7}{7 \times 7 \times 7} = \frac{7 \times 7}{1} = \frac{49}{1} = 49$$

$$3.3 \quad \frac{3^3 \cdot 2^4}{2^5 \cdot 3^2} = \frac{3 \times 3 \times 3 \times 2 \times 2 \times 2}{2 \times 2 \times 2 \times 2 \times 2 \times 3 \times 3} = \frac{3}{2}$$

$$3.4 \quad (5^2)^3 = (5^2)(5^2)(5^2) = 5 \times 5 \times 5 \times 5 \times 5 \times 5 = 5^6$$

$$4.1 \quad 2^{50} \cdot 2^{20} \\ = 2^{70}$$

$$4.2 \quad 3^2 \cdot 2^5 \cdot 3^8 \cdot 2^4 \\ = 3^{10} \cdot 2^9$$

$$4.3 \quad \frac{7^3 \cdot 5^2}{7^5 \cdot 5} \\ = \frac{5}{7^2} \\ = \frac{5}{49}$$

$$4.4 \quad \frac{2^{20} \cdot 3^{100}}{3^{50} \cdot 2^{80}} \\ = \frac{3^{50}}{2^{60}}$$

$$4.5 \quad 3^{11} \div 3^{20} \\ = \frac{3^{11}}{3^{20}} \\ = \frac{1}{3^9}$$

$$4.6 \quad (2^{12} \cdot 2^3) \div (2 \cdot 2^2) \\ = \frac{2^{12} \cdot 2^3}{2^1 \cdot 2^2} \\ = \frac{2^{15}}{2^3} \\ = \frac{2^{12}}{1} \\ = 2^{12}$$

$$4.8 \quad \frac{1}{(2^3)^4} \\ = \frac{1}{2^{12}}$$

$$4.9 \quad (3^2 \cdot 5^3)^2 \\ = 3^4 \cdot 5^6$$

$$4.10 \quad \frac{1}{(2^2 \cdot 7^8)^3} \\ = \frac{1}{26 \cdot 7^{24}}$$

$$4.11 \quad 3^0 \cdot 5^2 \\ = 1 \cdot 25$$

$$4.12 \quad 13^2 \cdot 13 \cdot 13^0 \\ = 13^2 \cdot 13^1 \cdot 1 \\ = 13^3$$

$$4.14 \quad 11^0 \div 11^{-3} \\ = \frac{11^0}{11^{-3}} \\ = \frac{1}{11^{-3}}$$

$$4.13 \quad 5^{-1} \cdot 5^{-3} \cdot 5^{-2} \\ = \frac{1}{5^1 \cdot 5^3 \cdot 5^2} \\ = \frac{1}{5^6}$$

$$4.15 \quad 5^{-5} \div 5^2$$

$$= \frac{5^{-5}}{5^2}$$

$$= \frac{1}{5^2 \cdot 5^5}$$

$$= \frac{1}{5^7}$$

$$4.17 \quad (2^{-3})^2$$

$$= \left(\frac{1}{2^3}\right)^2$$

$$= \frac{1^2}{(2^3)^2}$$

$$= \frac{1}{2^6}$$

$$4.19 \quad (5^4 \cdot 2^{-1})^2$$

$$= \left(\frac{5^4}{2^1}\right)^2$$

$$= \frac{(5^4)^2}{(2^1)^2}$$

$$= \frac{5^8}{2^2}$$

$$4.21 \quad (3^2)^2 \cdot 2^{-3}$$

$$= 3^4 \cdot 2^{-3}$$

$$= \frac{3^4}{2^3}$$

$$= \frac{81}{8}$$

$$4.23 \quad 4^3 \cdot 2^4$$

$$= (2^2)^3 \cdot 2^4$$

$$= 2^6 \cdot 2^4$$

$$= 2^{10}$$

$$\underline{2/16}$$

$$\underline{5/125}$$

$$\underline{2/48}$$

$$\underline{2/60}$$

$$\underline{3/81}$$

$$\underline{2/8}$$

$$\underline{5/25}$$

$$\underline{2/24}$$

$$\underline{2/30}$$

$$\underline{3/27}$$

$$\underline{2/4}$$

$$\underline{5/5}$$

$$\underline{2/12}$$

$$\underline{3/15}$$

$$\underline{3/9}$$

$$\underline{2/2}$$

$$\underline{/1}$$

$$\underline{2/6}$$

$$\underline{5/5}$$

$$\underline{3/3}$$

$$\underline{/1}$$

$$\underline{3/3}$$

$$\underline{/1}$$

$$\underline{/1}$$

$$\underline{/1}$$

$$16 = 2 \times 2 \times 2 \times 2$$

$$= 2^4$$

$$125 = 5 \times 5 \times 5$$

$$= 5^3$$

$$48 = 2 \times 2 \times 2 \times 2 \times 3$$

$$= 2^4 \cdot 3^1$$

$$60 = 2 \times 2 \times 3 \times 5$$

$$= 2^2 \cdot 3^1 \cdot 5^1$$

$$81 = 3 \times 3 \times 3 \times 3$$

$$= 3^4$$

$$4.24 \quad 16^3 \cdot 2^2 = (2^4)^3 \cdot 2^2 = 2^{12} \cdot 2^2 = 2^{14}$$

$$4.25 \quad 125^5 \cdot 5^{-2} = (5^3)^5 \cdot 5^{-2} = \frac{5^{15}}{5^2} = \frac{5^{13}}{1} = 5^{13}$$

$$4.26 \quad 48^4 \cdot 3^2 = (2^4 \cdot 3^1)^4 \cdot 3^2 = 2^{16} \cdot 3^4 \cdot 3^2 = 2^{16} \cdot 3^6$$

$$4.27 \quad 60^8 \cdot 2^{-4} = (2^2 \cdot 3^1 \cdot 5^1)^8 \cdot 2^{-4} = \frac{2^{16} \cdot 3^8 \cdot 5^8}{2^4} = \frac{2^{12} \cdot 3^8 \cdot 5^8}{1} = 2^{12} \cdot 3^8 \cdot 5^8$$

$$4.28 \quad \frac{1}{81^6} \cdot 3^4 = \frac{1}{(3^4)^6} \cdot \frac{3^4}{1} = \frac{1}{3^{24}} \cdot \frac{3^4}{1} = \frac{1}{3^{20}}$$

$$5.1 \quad 2,83 \times 10^3 = 2830$$

$$5.3 \quad 3,025 \times 10^4 = 30250$$

$$5.5 \quad 3,25 \times 10^4 \times 10^{-3} = 3,25 \times 10^1 = 32,5$$

$$6.1 \quad 10000 = 575$$

$$= 10000,0$$

$$= 1,0 \times 10^4 \quad 6.2 \quad 0,0876 = 8,76 \times 10^{-2}$$

$$6.3 \quad 125,346 = 1,25346 \times 10^2$$

$$6.5 \quad \frac{23,457}{10^{-2}} = 23,457 \times 10^2 = 2,3457 \times 10^{2+1} = 2,3457 \times 10^3$$

$$5.7 \quad 365,342 \times 10^3 = 3,65342 \times 10^{3+2}$$

$$= 3,65342 \times 10^5 \quad 6.8 \quad 0,000456 \times 10^8 = 4,56 \times 10^{8-4} = 4,56 \times 10^4$$

$$7. \quad \frac{3,56 \times 10^{-8}}{200 \times 10^{-3}} = 0,000000178 = 1,78 \times 10^{-7}$$

$$8.1 \quad \frac{2^{100} \times 2^{50}}{2^{140}} = \frac{2^{100+50}}{2^{140}} = \frac{2^{150}}{2^{140}} = 2^{10}$$

$$9. \quad \sqrt[5]{\frac{20+0,34}{200-25,05}} + 8 = 8,650260 \dots \dots \simeq 8,65$$

$$10. \quad 0,000058346 \times 10^8 = 5,8346 \times 10^{8-5} = 5,8346 \times 10^3$$

$$11. \quad 5,026 \times 10^3 = 5026$$

$$12. \quad 0,0038 = 3,8 \times 10^{-3}$$

$$\begin{aligned}13. \quad & \frac{3 \times 10^7 \times 14 \times 10^2}{21 \times 10^5} \\&= \frac{3 \times 2 \times 7 \times 10^7 \times 10^2}{3 \times 7 \times 10^5} \\&= \frac{2 \times 10^9}{10^5} \\&= 2,0 \times 10^4\end{aligned}$$

$$\begin{aligned}15. \quad & \frac{2^{-2}}{3^{-2}} \\&= \frac{3^2}{2^2} \\&= \frac{9}{4}\end{aligned}$$

$$\begin{aligned}14.1 \quad & \frac{2^{100} \times 2^{50}}{2^{120}} \\&= \frac{2^{150}}{2^{120}} \\&= 2^{30}\end{aligned}$$

$$\begin{aligned}14.2 \quad & (2^3 \cdot 3^2)^4 \\&= 2^{12} \cdot 3^8\end{aligned}$$

Hoofstuk 1

Getalle, Bewerkings en Verwantskappe

Antwoorde 1D: Magte en wortels

1. $\sqrt{64}$

$= \sqrt{8^2}$

$= 8^{\frac{2}{2}}$

$= 8$

2. $\sqrt{4} + \sqrt{9}$

$= \sqrt{2^2} + \sqrt{3^2}$

$= 2^{\frac{2}{2}} + 3^{\frac{2}{2}}$

$= 2 + 3 = 5$

3. $3\sqrt{36}$

$= 3\sqrt{6^2}$

$= 3 \cdot 6^{\frac{2}{2}}$

$= 3 \cdot 6 = 18$

4. $4\sqrt{9} + \sqrt{36} \div 2$

$= 4 \cdot \sqrt{3^2} + \sqrt{6^2} \div 2$

$= 4 \cdot 3^{\frac{2}{2}} + 6^{\frac{2}{2}} \div 2$

$= 4 \cdot 3 + 6 \div 2$

$= 12 + 3 = 15$

5. $\sqrt{2\frac{7}{9}}$

$= \sqrt{\frac{25}{9}}$

$= \frac{\sqrt{5^2}}{\sqrt{3^2}}$

$= \frac{5^{\frac{2}{2}}}{3^{\frac{2}{2}}}$

$= \frac{5}{3}$

6. $\sqrt{3^2 + 4^2}$

$= \sqrt{9 + 16}$

$= \sqrt{25}$

$= \sqrt{5^2}$

$= 5^{\frac{2}{2}}$

$= 5$

7. $\sqrt{25 \times 4 \times 36}$

$= \sqrt{5^2} \times \sqrt{2^2} \times \sqrt{6^2}$

$= 5^{\frac{2}{2}} \times 2^{\frac{2}{2}} \times 6^{\frac{2}{2}}$

$= 5 \times 2 \times 6$

$= 60$

8. $\sqrt{\sqrt{81}}$

$= \sqrt{\sqrt{9^2}}$

$= \sqrt{9^{\frac{2}{2}}}$

$= \sqrt{9}$

$= \sqrt{3^2}$

$= 3^{\frac{2}{2}} = 3$

9. $\sqrt{0,0025}$

$= \sqrt{\frac{25}{10000}}$

$= \sqrt{\frac{1}{400}}$

$= \frac{\sqrt{1}}{\sqrt{20^2}}$

$= \frac{1}{20}$

10. $(2 \times 3)^2$

$= (6)^2$

$= 36$

11. $\sqrt[3]{27}$

$= \sqrt[3]{(3)^3}$

$= (3)^{\frac{3}{3}}$

$= 3$

12. $\sqrt[3]{64} + \sqrt{36}$

$= \sqrt[3]{4^3} + \sqrt{6^2}$

$= 4^{\frac{3}{3}} + 6^{\frac{2}{2}}$

$= 4 + 6 = 10$

13. $2^3 + 1^3$

$= 8 + 1$

$= 9$

14. $\sqrt[3]{3^6 \cdot 2^3}$

$= 3^{\frac{6}{3}} \cdot 2^{\frac{3}{3}}$

$= 3^2 \cdot 2$

$= 9 \cdot 2 = 18$

15. $\sqrt{49} \times \sqrt[3]{8}$

$= \sqrt{7^2} \times \sqrt[3]{2^3}$

$= 7^{\frac{2}{2}} \times 2^{\frac{3}{3}} = 7 \times 2 = 14$

16. $(6 - 2)^3 + (11 - 7)^3$

$= (4)^3 + (4)^3$

$= 64 + 64 = 128$

17. $\sqrt[3]{\sqrt{64}}$

$$= \sqrt[3]{4^3}$$

$$= \sqrt{4^{\frac{3}{2}}}$$

$$= \sqrt{4}$$

$$= \sqrt{2^2}$$

$$= 2^{\frac{2}{2}} = 2$$

$$19. \quad 4\sqrt[3]{8} - 2\sqrt{16}$$

$$= 4 \cdot \sqrt[3]{2^3} - 2 \cdot \sqrt{4^2}$$

$$= 4 \cdot 2^{\frac{3}{3}} - 2 \cdot 4^{\frac{2}{2}}$$

$$= 4 \cdot 2 - 2 \cdot 4$$

$$= 8 - 8 = 0$$

$$18. \quad \sqrt{4} \left(\sqrt{4} + \sqrt[3]{8} \right)$$

$$= \sqrt{2^2} \left(\sqrt{2^2} + \sqrt[3]{2^3} \right)$$

$$= 2^{\frac{2}{2}} \left(2^{\frac{2}{2}} + 2^{\frac{3}{3}} \right)$$

$$= 2(2+2)$$

$$= 2(4) = 8$$

$$20. \quad 2\sqrt[3]{125}$$

$$= 2 \cdot \sqrt[3]{(5)^3}$$

$$= 2 \cdot \left(5^{\frac{3}{3}} \right)$$

$$= 2 \cdot 5$$

$$= 10$$

$$22. \quad \left((\sqrt{4})^2 \right)^3$$

$$= \left((\sqrt{4})^2 \right)^3$$

$$= (4)^3$$

$$21. \quad \sqrt{36} \times \sqrt{4} + \sqrt[3]{27} - \sqrt{1}$$

$$= \sqrt{6^2} \times \sqrt{2^2} + \sqrt[3]{3^3} - \sqrt{1}$$

$$= 6 \times 2 + 3 - 1$$

$$= 12 + 2 = 14$$

$$24. \quad \sqrt{-9}$$

geen \mathbb{R} oplossing

$$23. \quad \sqrt{3} \cdot \sqrt{3} \cdot \sqrt{3} \cdot \sqrt{3}$$

$$= (\sqrt{3})^2 \cdot (\sqrt{3})^2$$

$$= 3 \cdot 3 = 9$$

$$26. \quad \sqrt{\frac{18}{50}}$$

$$= \sqrt{\frac{9}{25}}$$

$$= \frac{\sqrt{3^2}}{\sqrt{5^2}}$$

$$25. \quad \frac{\sqrt{144}}{4}$$

$$= \frac{3}{5}$$

$$= \frac{\sqrt{12^2}}{4}$$

$$= \frac{12}{4} = 3$$

$$27. \quad \sqrt{3\frac{3}{5} - 1\frac{1}{25}}$$

$$= \sqrt{\frac{18}{5} - \frac{26}{25}}$$

$$= \sqrt{\frac{90-26}{25}}$$

$$= \sqrt{\frac{64}{25}}$$

$$= \frac{\sqrt{8^2}}{\sqrt{5^2}} = \frac{8}{5}$$

$$28. \quad (\sqrt{5})^2 + (2\sqrt{3})^2$$

$$= 5 + 4 \cdot 3$$

$$= 5 + 12 = 17$$

$$29. \quad \sqrt[3]{25^5} + (2)^5 - (\sqrt[8]{8})^8 - (5-4)^{100}$$

$$= 25^{\frac{5}{3}} + 32 - 8^{\frac{8}{8}} - 1^{100}$$

$$= 25 + 32 - 8 - 1 = 48$$

$$30. \quad \sqrt{7056} \quad 2\lfloor 7056$$

$$= \sqrt{2^4 \cdot 3^2 \cdot 7^2}$$

$$2\lfloor 3528$$

$$= 2^{\frac{4}{2}} \cdot 3^{\frac{2}{2}} \cdot 7^{\frac{2}{2}}$$

$$2\lfloor 1764$$

$$= 2^2 \cdot 3 \cdot 7$$

$$2\lfloor 882$$

$$= 4 \cdot 3 \cdot 7$$

$$3\lfloor 441$$

$$= 84$$

$$3\lfloor 147$$

$$7\lfloor 49$$

$$7\lfloor 7$$

$$\lfloor 1$$

$$32. \quad \sqrt{1024}$$

$$2\lfloor 1024$$

$$= \sqrt{2^{10}}$$

$$2\lfloor 512$$

$$= 2^{\frac{10}{2}}$$

$$2\lfloor 256$$

$$= 2^5$$

$$2\lfloor 128$$

$$= 32$$

$$2\lfloor 64$$

$$2\lfloor 32$$

$$2\lfloor 16$$

$$2\lfloor 8$$

$$2\lfloor 4$$

$$2\lfloor 2$$

$$\lfloor 1$$

$$33. \quad \sqrt[3]{3375}$$

$$3\lfloor 3375$$

$$= \sqrt[3]{3^3 \cdot 5^3}$$

$$3\lfloor 1125$$

$$= 3^{\frac{3}{3}} \cdot 5^{\frac{3}{3}}$$

$$3\lfloor 375$$

$$= 3.5$$

$$5\lfloor 125$$

$$= 15$$

$$5\lfloor 25$$

$$5\lfloor 5$$

$$\lfloor 1$$

$$34.1 \quad \sqrt{16+9}$$

$$= \sqrt{25}$$

$$= 5$$

$$34.2 \quad \sqrt{36 \cdot 64}$$

$$= \sqrt{36} \cdot \sqrt{64}$$

$$= 6.8$$

$$= 48$$

$$34.3 \quad \sqrt[3]{3^6 \cdot 2^9}$$

$$= 3^{\frac{6}{3}} \cdot 2^{\frac{9}{3}}$$

$$= 3^2 \cdot 2^3$$

$$= 9 \cdot 8$$

$$= 72$$

$$34.4 \quad \sqrt{(161)^2}$$

$$= 161^{\frac{2}{2}}$$

$$= 161$$

$$34.6 \quad 1^5 + 1^4$$

$$= 1 + 1$$

$$= 2$$

$$34.5 \quad \sqrt[3]{5^3}$$

$$= 5$$

$$34.7 \quad 2^3 \cdot 3^2$$

$$\begin{aligned} &= 8.9 \\ &= 72 \end{aligned}$$

$$34.8 \quad \frac{2^{-3}}{3^{-2}}$$

$$\begin{aligned} &= \frac{3^2}{2^3} \\ &= \frac{9}{8} \end{aligned}$$

$$2 \lfloor 1728$$

$$35.1 \quad \sqrt{9801}$$

$$= \sqrt{3^4 \cdot 11^2}$$

$$= 3^{\frac{4}{2}} \cdot 11^{\frac{2}{2}}$$

$$= 3^2 \cdot 11$$

$$= 9 \cdot 11$$

$$= 99$$

$$3 \lfloor 9801$$

$$3 \lfloor 3267$$

$$3 \lfloor 1089$$

$$3 \lfloor 363$$

$$11 \lfloor 121$$

$$11 \lfloor 11$$

$$\lfloor 1$$

$$35.2 \quad \sqrt[3]{1728}$$

$$= \sqrt[3]{2^6 \cdot 3^3}$$

$$= 2^{\frac{6}{3}} \cdot 3^{\frac{3}{3}}$$

$$= 2^2 \cdot 3$$

$$= 4 \cdot 3$$

$$= 12$$

$$2 \lfloor 864$$

$$2 \lfloor 432$$

$$2 \lfloor 216$$

$$2 \lfloor 108$$

$$2 \lfloor 54$$

$$3 \lfloor 27$$

$$3 \lfloor 9$$

$$3 \lfloor 3$$

$$\lfloor 1$$

$$35.3 \quad \sqrt{21 \times 18 \times 42}$$

$$= \sqrt{3 \times 7 \times 2 \times 3^2 \times 2 \times 3 \times 7}$$

$$= \sqrt{3^4 \times 7^2 \times 2^2}$$

$$= 3^{\frac{4}{2}} \cdot 7^{\frac{2}{2}} \cdot 2^{\frac{2}{2}}$$

$$= 3^2 \cdot 7 \cdot 2$$

$$= 9 \cdot 7 \cdot 2$$

$$= 126$$

$$3 \lfloor 21$$

$$2 \lfloor 18$$

$$2 \lfloor 42$$

$$7 \lfloor 7$$

$$3 \lfloor 9$$

$$3 \lfloor 21$$

$$\lfloor 1$$

$$3 \lfloor 3$$

$$7 \lfloor 7$$

$$\lfloor 1$$

$$\lfloor 1$$

$$= 9 \cdot 7 \cdot 2$$

$$= 2916$$

$$2 \lfloor 2916$$

$$2 \lfloor 1458$$

$$36. \quad \sqrt{2916}$$

$$= \sqrt{2^2 \cdot 3^6}$$

$$= 2^{\frac{2}{2}} \cdot 3^{\frac{6}{2}}$$

$$= 2 \cdot 3^3$$

$$= 2 \cdot 27$$

$$= 54$$

$$3 \lfloor 729$$

$$3 \lfloor 243$$

$$3 \lfloor 81$$

$$3 \lfloor 27$$

$$3 \lfloor 9$$

$$3 \lfloor 3$$

$$\lfloor 1$$

$$37. \quad \sqrt[3]{5832}$$

$$= \sqrt[3]{2^3 \cdot 3^6}$$

$$= 2^{\frac{3}{3}} \cdot 3^{\frac{6}{3}}$$

$$= 2 \cdot 3^2$$

$$= 2 \cdot 9$$

$$= 18$$

$$2 \lfloor 5832$$

$$2 \lfloor 2916$$

$$2 \lfloor 1458$$

$$3 \lfloor 729$$

$$3 \lfloor 243$$

$$3 \lfloor 81$$

$$3 \lfloor 27$$

$$3 \lfloor 9$$

$$3 \lfloor 3$$

$$\lfloor 1$$

$$38.1 \quad \sqrt[3]{-64} + 3^3$$

$$38.2 \quad 2187 \div 3^3$$

$$3 \lfloor 2187$$

$$\begin{aligned}
 &= \sqrt[3]{(-4)^3} + 27 &= \frac{2187}{3^3} & 3 \mid 729 \\
 &= -4 + 27 &= \frac{3^7}{3^3} & 3 \mid 243 \\
 &= 23 &= 3^4 & 3 \mid 81 \\
 &&= 81 & 3 \mid 27
 \end{aligned}$$

$$\begin{aligned}
 38.3 \quad & (-8 \times 2)^2 - (8 + 2)^2 & 3 \mid 9 \\
 &= (-16)^2 - (16)^2 & 3 \mid 3 \\
 &= 256 - 256 & \lfloor 1 \\
 &= 0
 \end{aligned}$$

$$\begin{aligned}
 38.4 \quad & (-6 - 1)^2 - \sqrt[3]{8} \\
 &= (-7)^2 - \sqrt[3]{2^3}
 \end{aligned}$$

$$\begin{aligned}
 38.5 \quad & \sqrt[3]{0,008} \\
 &= \sqrt[3]{\frac{8}{1000}} \\
 &= \frac{\sqrt[3]{1}}{\sqrt[3]{125}} \\
 &= \frac{1}{\sqrt[3]{5^3}} \\
 &= \frac{1}{5}
 \end{aligned}$$

$$\begin{aligned}
 38.6 \quad & \sqrt{0,16} + \frac{3}{5} \\
 &= \sqrt{\frac{16+4}{100+4}} + \frac{3}{5}
 \end{aligned}$$

$$\begin{aligned}
 38.7 \quad & \sqrt{2^4 + 3^2} \\
 &= \sqrt{16 + 9} \\
 &= \sqrt{25} \\
 &= \sqrt{5^2} \\
 &= 5
 \end{aligned}$$

$$\begin{aligned}
 38.8 \quad & 1^3 \times (-4)^3 \div (2 \times 2^2) \\
 &= 1 \times \frac{-64}{8}
 \end{aligned}$$

$$\begin{aligned}
 &= 1 \times -8 \\
 &= -8
 \end{aligned}$$

$$\begin{aligned}
 38.10 \quad & \frac{\sqrt[3]{125} - \sqrt{16}}{2^5 - (3^3 + 2^2)} \\
 &= \frac{\sqrt[3]{5^3} - \sqrt{4^2}}{32 - (27 + 4)}
 \end{aligned}$$

$$= 16$$

$$\begin{aligned}
 38.11 \quad & \sqrt[3]{\frac{125}{216}} + \frac{1}{6} \\
 &= \sqrt[3]{\frac{5^3}{6^3}} + \frac{1}{6} \\
 &= \frac{5}{6} + \frac{1}{6}
 \end{aligned}$$

$$38.12 \quad (-1)^{10} + 5 - 3 = 1 + 5 - 3 = 3$$

$$= \frac{6}{6}$$

$$38.13 \quad \sqrt[3]{2^{15} \cdot 3^{27}} = 2^{15 \div 3} \cdot 3^{27 \div 3} = 2^5 \cdot 3^9$$

$$= 1$$

Meer oor “Wiskunde Anibrand Antwoordboek Graad 8” en die outeur.

Ek is reeds vir 28 jaar betrokke by Wiskunde-onderrig vir graad 8 tot graad 12 leerders. Die afgelope 10 jaar is ek verbonde aan Hoërskool Die Wilgers in Pretoria, waar ek ‘n Wiskunde Akademie bedryf met een groep in elke graad.

Met die aanvang van die nuwe KABV sillabus in 2007 het ek begin om al my notas vir my Wiskunde-onderrig elektronies saam te stel met behulp van innoverende sagteware sodat dit alle onderwerpe met grafika en voorbeelde volledig verduidelik. Die graad 8 Wiskunde Anibrand Antwoordboek bied volledig uitgewerkte, verduidelikende antwoorde vir al die huiswerk probleme in die graad 8 “Wiskunde Anibrand Notaboek”.

Leerders wat hierdie boek gebruik om hulle huiswerk probleme te merk, kan uit die antwoorde self sien waar hulle gefouteer het en dan hulle foute korrigeer.

Ek gebruik hierdie antwoorde die afgelope 5 jaar in my klasaanbieding vir die graad 8 leerders. Dit stel my in staat om die antwoorde konstant te verbeter, soos wat ek dit in die klassituasie as nodig ervaar.

Die volledige antwoord op huiswerprobleme help leerders om selfvertroue in die vak te kry want hulle kan hulle probleme identifiseer wanneer hulle huiswerk doen, dit uitsorteer en dan voortgaan met die res van die huiswerk probleme.

Hierdie boek, saam met die Notaboek, is die antwoord vir alle graad 8 leerders wat wil presteer in Wiskunde en ook vir alle Wiskunde onderwysers wat sonder moeite ‘n kwaliteit Wiskunde klasaanbieding vir leerders wil bied.

www.wiskundeanibrand.com